

Molecular Mechanics

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Outline

1. Molecular Mechanics (MM)
2. Quantum Mechanics (QM)
3. Solvent Representation

Molecular Mechanics (MM)

Simplified theoretical description of molecules based on classical mechanics (= “dead-man potential”)

Hooke’s law (died 1703) – spring stiffness

Coulomb’s law (d. 1806) - electrostatics

Force-fields – CHARMM, AMBER, GROMOS, CVFF, MMFF,

$$E_{MM} = E_{\text{bond}} + E_{\text{nonbond}}$$

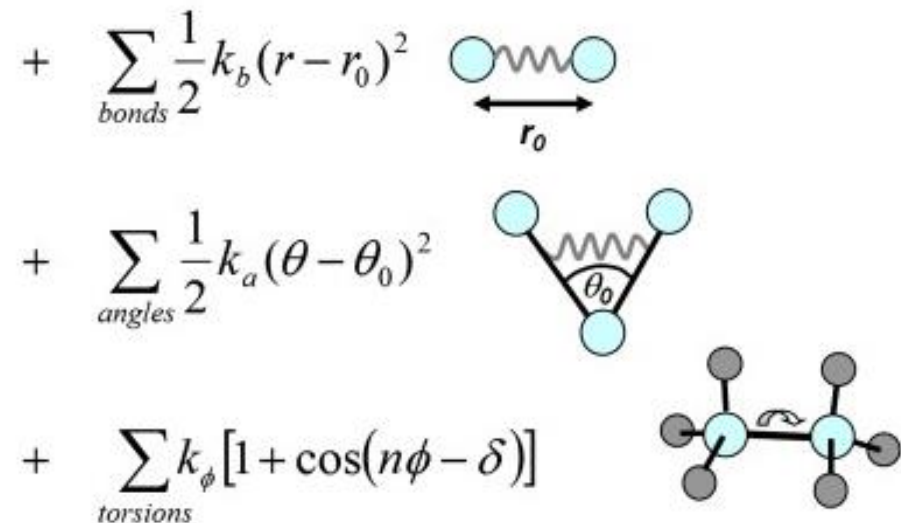
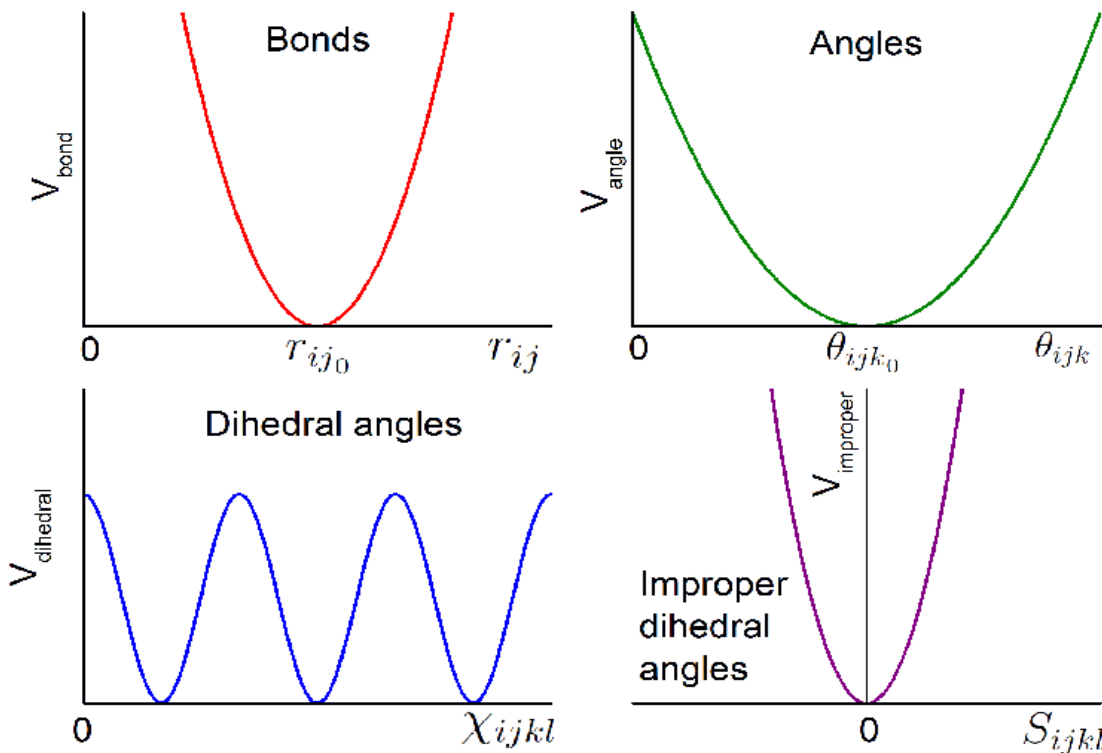
Nobel Prize in Chemistry, 2013 (Karplus, Warshel, Levitt)

MM - Bonded Terms

Atom = mass

Molecule = atoms connected by springs

$$E_{\text{bonded}} = E_{\text{bond}} + E_{\text{angle}} + E_{\text{dihed}} + E_{\text{improper}}$$



MM - Nonbonded Terms

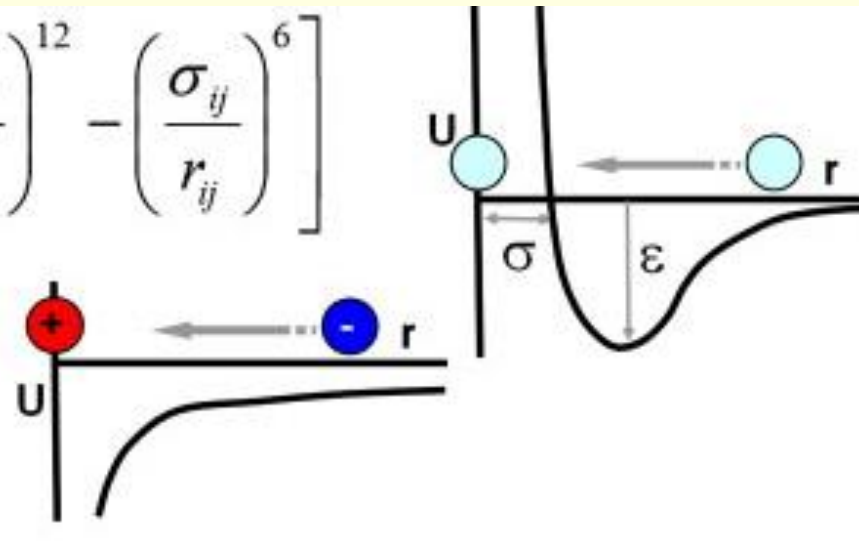
Electrostatic: Coulomb

van der Waals: Dispersion

$$E_{\text{nonbond}} = E_{\text{Coulomb}} + E_{\text{vdW}}$$

$$U = \sum_{i < j} \sum 4\epsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^6 \right]$$

$+ \sum_{i < j} \sum \frac{q_i q_j}{4\pi\epsilon_0 r_{ij}}$



The diagram illustrates the nonbonded energy terms. The top part shows a Lennard-Jones potential well with parameters σ and ϵ , and a corresponding diagram of two particles (red and blue) with distance r . The bottom part shows the Coulomb potential with a corresponding diagram of two charged particles (red and blue) with distance r .

Molecular Dynamics

- simulating molecular movements
- solving Newton's equations of motion for nuclei in MM (electrons as parameters)

$$\begin{aligned}-dE/dx &= \mathbf{F} \\ &= \mathbf{m} * \mathbf{a} \\ &= m * dv/dt \\ &= m * (dx/dt)/dt\end{aligned}$$

Trajectory – x (coordinate frames)

Velocity - v (t)

Quantum Mechanics (QM)

mathematical description of particle-wave duality of electrons

Time-independent Schrödinger equation: $\hat{H}\psi = E\psi$

\hat{H} – Hamilton operator

ψ - Wave function

E – energy

Heisenberg's uncertainty principle

Position, x , and momentum, p of a particle cannot be determined precisely

Probability distributions

Quantum Chemistry

Application of QM to chemistry

Wave model of atom: positively charged nucleus surrounded by clouds of electrons in **atomic orbitals**

Quantum numbers

Pauli Exclusion Principle – two electrons in one orbital differ by their spin

Hund's Rules – determine the ground state of an atom

Aufbau Principle – order by which electrons occupy orbitals

Atomic Orbitals: linear combinations → Molecular Orbitals

- Basis sets

Basis Sets

Set of functions → representations of molecular orbitals
(MO-LCAO)

Slater - Gaussian

- Minimal basis set (one function per orbital)
 - Polarization functions
 - Diffuse functions
-
- STO-3G, 3-21G, 6-31G*, 6-311+G**, SVP, aug-cc-pVTZ

Ab initio QM methods ("from first principles")

Approximations for molecules of >3 atoms

Born-Oppenheimer approximation: separates movement of nuclei and electrons

Hartree-Fock – electronic effects as mean field, H-bond described, not dispersion (electron correlation)

Møller-Plesset perturbation theory (MP2, MP3,)

CCSD(T) – coupled-cluster, singles doubles triples

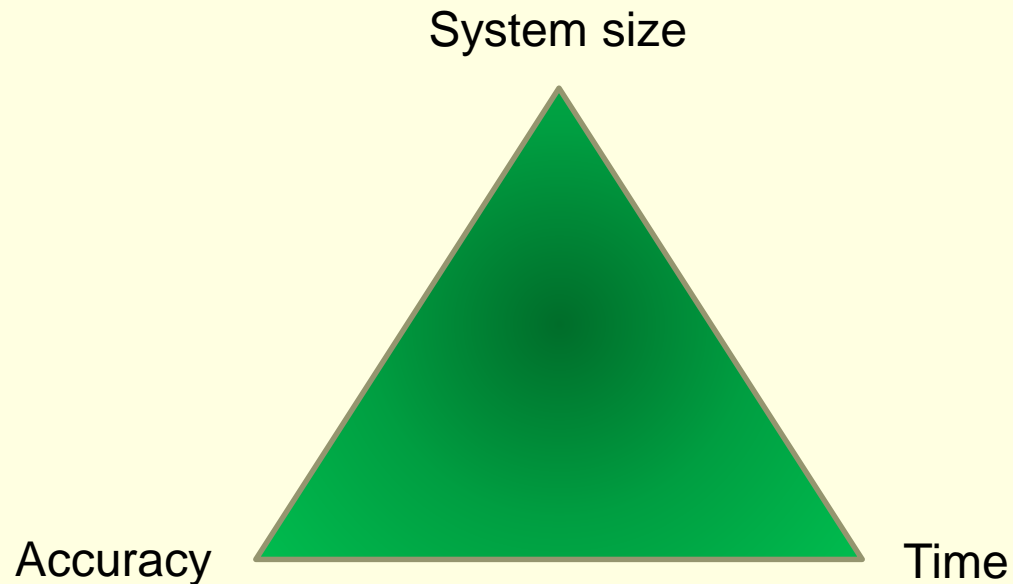
Scaling – HF (N^4), MP2 (N^5), CCSD(T) (N^6)

Quantum Chemistry

Covalent Reactions – electron rearrangements

Noncovalent Interactions

- proton/charge transfer
- sigma-hole bonding
- metals
- ligands (no parametrization)



Density Functional Theory (DFT)

Alternative (non- ψ) description

Electron Density

Partial description of dispersion

Exchange-correlation Functionals: B3LYP, PBE, BP86, M06

Missing Dispersion - Empirical

Semiempirical QM

Integrals – parameters

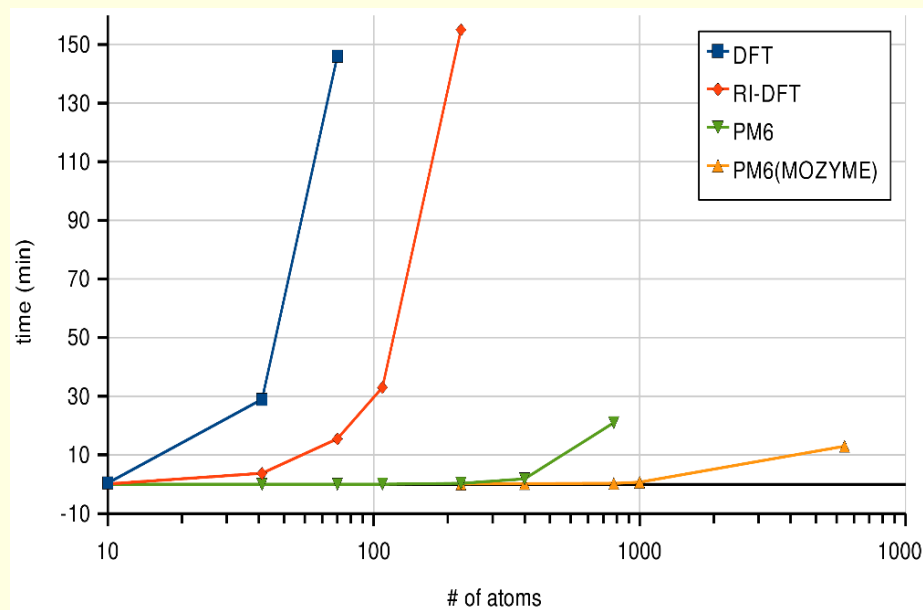
Simplified HF, no dispersion

AM1, PM6 - MOPAC

SCC-DF-TB

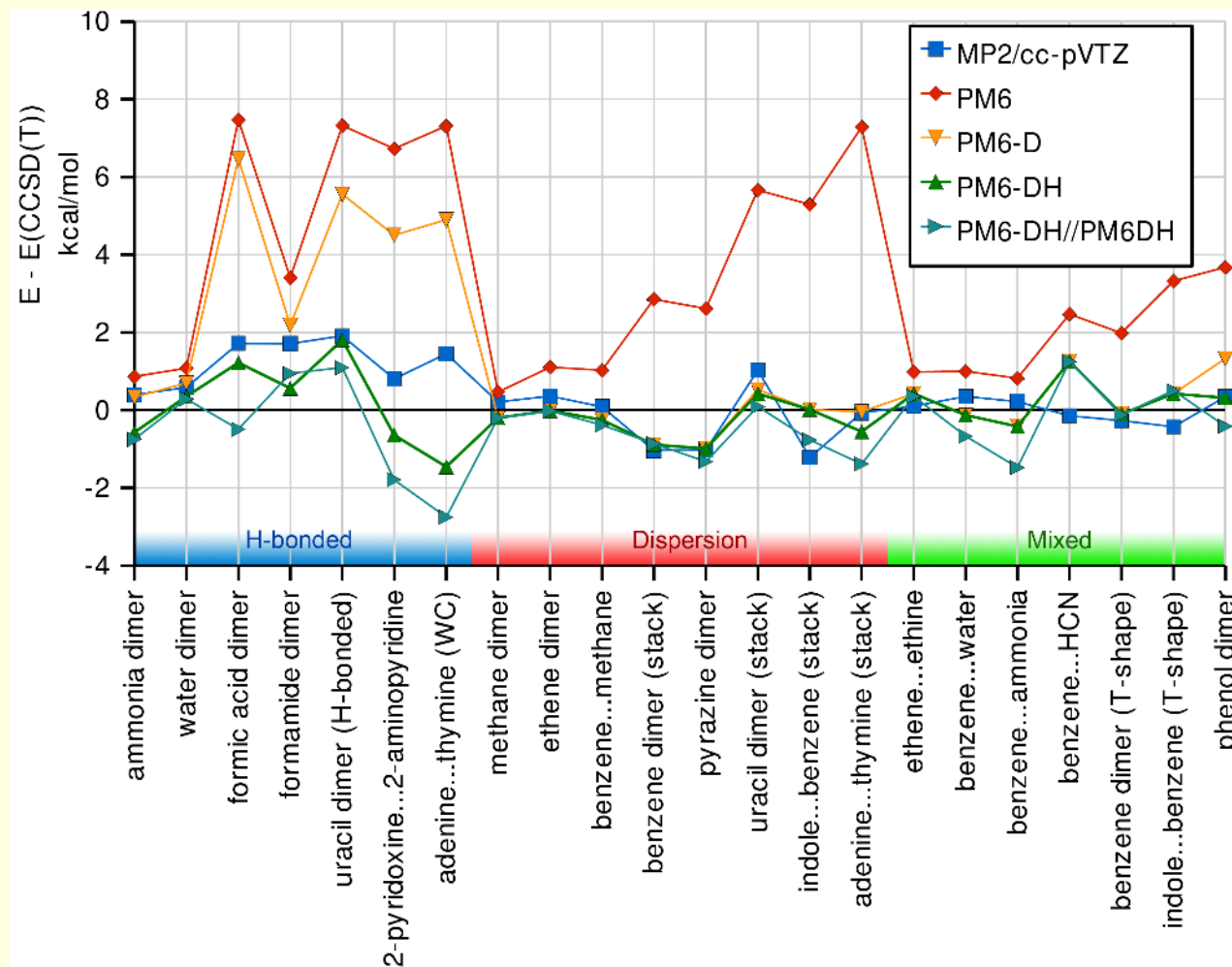
Linear scaling (N): MOZYME

Underestimate H-bonds, repulsion subminimal basis, only valence orbitals, core-core



Corrected Semiempirical QM

D3H4X – reliable: corrections for H-bonding, D-dispersion, X-bonding



Řezáč, ..., Hobza *J. Chem. Theory Comput.* **2009**, 5, 1749

Řezáč, Hobza, *Chem. Phys. Lett.* **2011**, 506, 286

Řezáč, Hobza, *J. Chem. Theory Comput.* **2012**, 8, 141

Parametrization

Model systems

Consistent Datasets CCSD(T)/CBS

H-bonding, dispersion, stacking (S22, S66)

Nonequilibrium geometries (S22x5, S66x8)

X-bonding (X40)

Large dispersion (L7)

Solvent Representation

Explicit

- MM: TIP3P, SPC, TIP5P, SPC/E
- QM: H_3O^+ , OH^-

Implicit = Continuum

- MM: generalized Born, Poisson-Boltzmann
- QM: PCM, COSMO, SMD

Solvation Free Energy

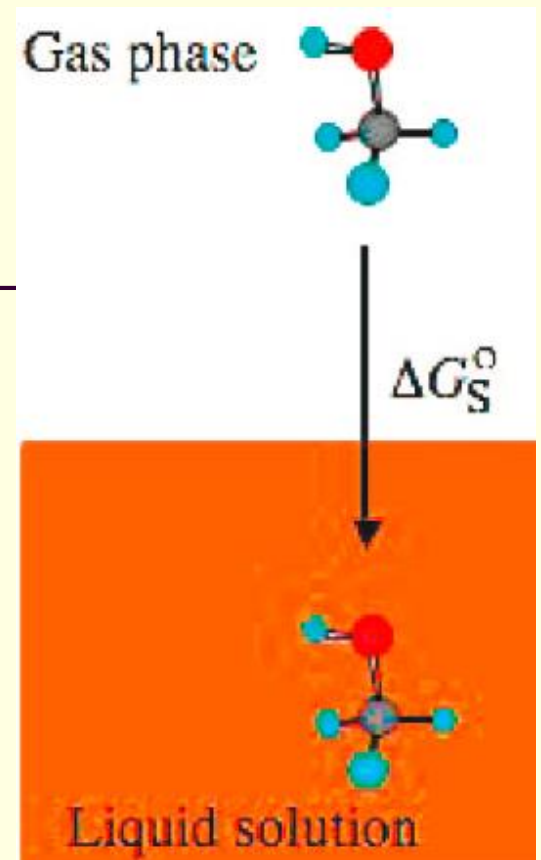
$$\Delta G_S^{\circ}(A) = \lim_{[A]_{\text{sol}} \rightarrow 0} \left\{ -RT \ln \frac{[A]_{\text{sol}}}{[A]_{\text{gas}}} \Big|_{\text{eq}} \right\}$$

Implicit = Continuum

- Damping of electrostatic interactions

Explicit

- specific H-bonds



Conclusions

1. Molecular Mechanics (MM)
2. Quantum Mechanics (QM)
3. Solvent Representations